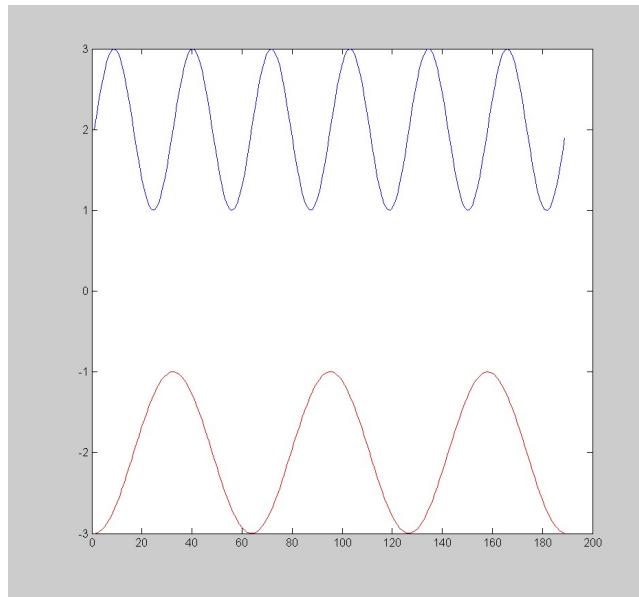


# Gradient Domain blending (1D)

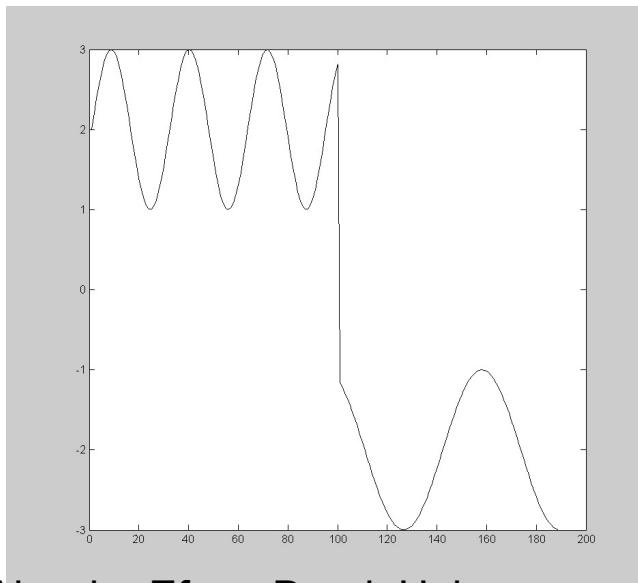
Two signals



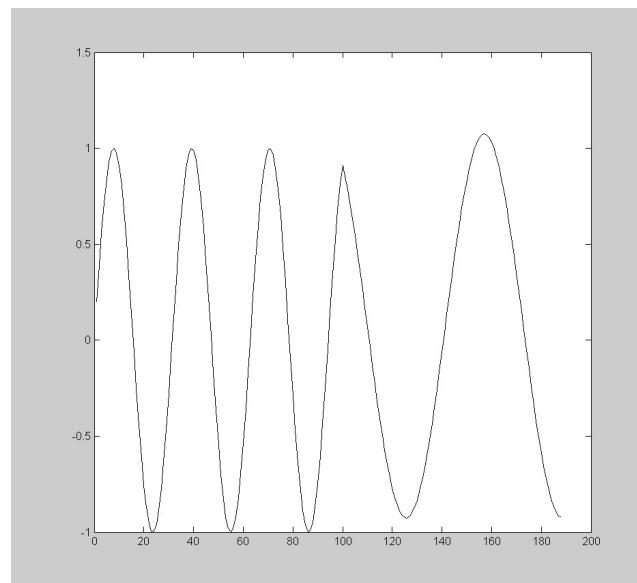
bright

dark

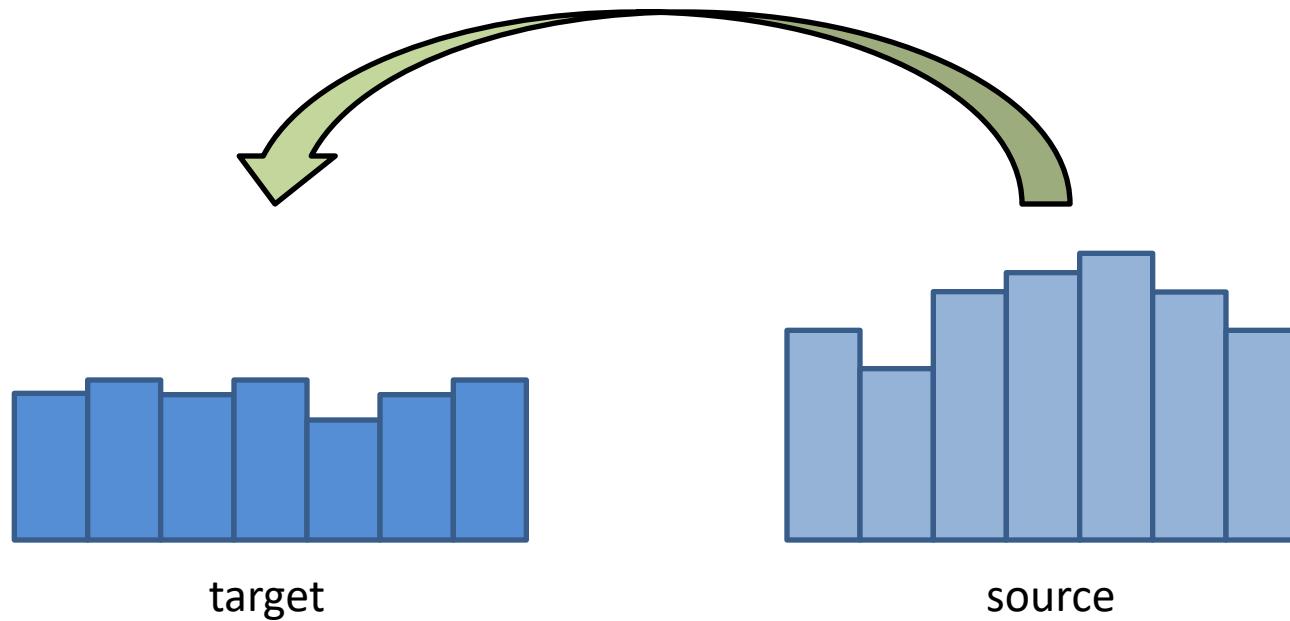
Regular blending



Blending derivatives

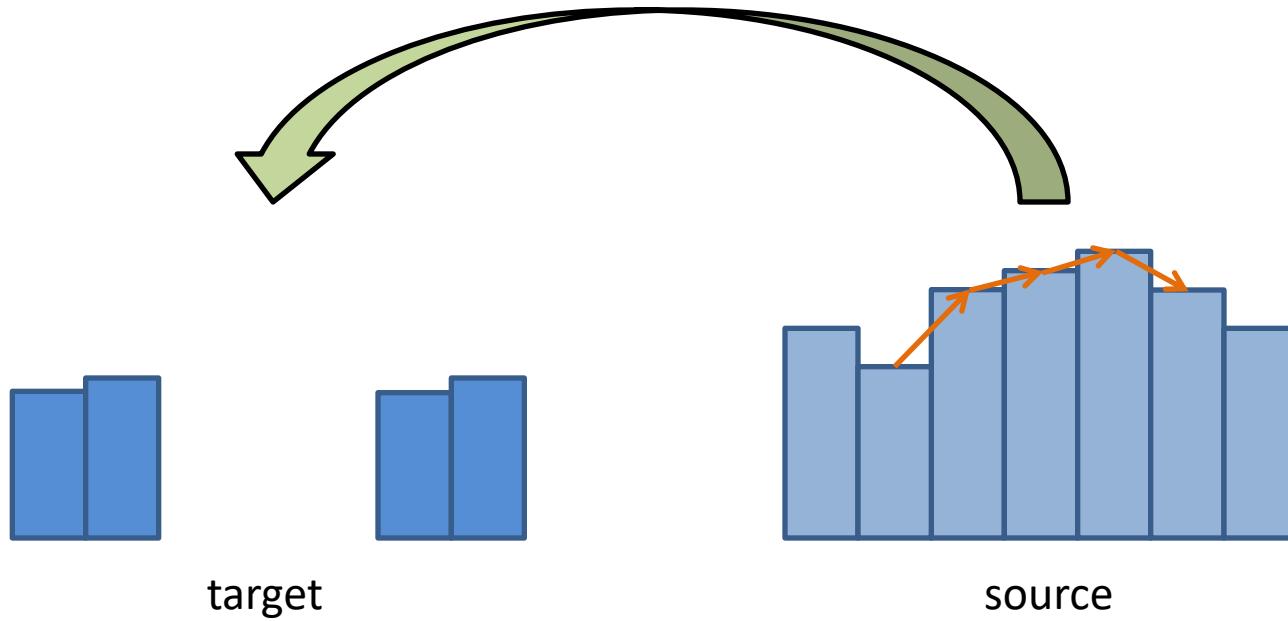


# Gradient hole-filling (1D)



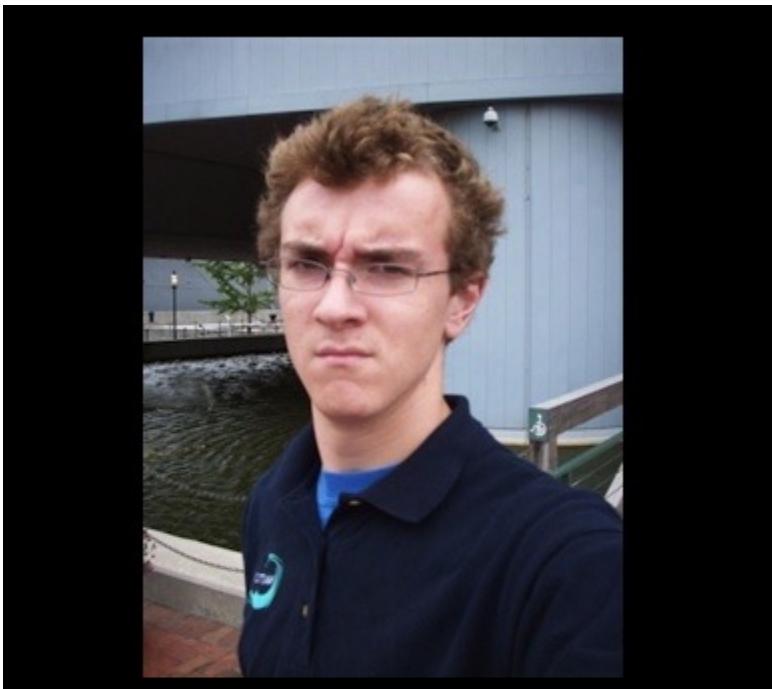
target

source



It is impossible to faithfully preserve the gradients

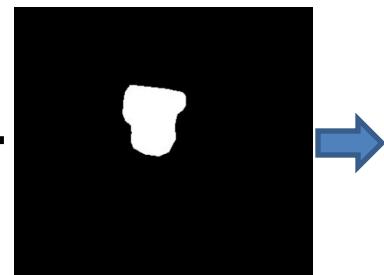
# Example



Gradient Visualization



+



Specify object  
region



# Poisson Blending Algorithm

A good blend should preserve gradients of source region without changing the background

Treat pixels as variables to be solved

$v$ : output pixels

- Minimize squared difference between gradients of foreground region and gradients of target region
- Keep background pixels constant

$$v = \arg \min_v \sum_{i \in S, j \in N_i \cap S} ((v_i - v_j) - (s_i - s_j))^2 + \sum_{i \in S, j \in N_i \cap \neg S} ((v_i - t_j) - (s_i - s_j))^2$$

↑  
Target (background)  
↓  
Source (foreground)

Output

- $i$  current pixel's index
- $N_i$  Current pixel's neighbors
- $j$  neighbor pixel index
- $S, \neg S$  foreground/background mask

# Examples

## Gradient domain processing

$$\mathbf{v} = \arg \min_{\mathbf{v}} \sum_{i \in S, j \in N_i \cap S} ((v_i - v_j) - (s_i - s_j))^2 + \sum_{i \in S, j \in N_i \cap \neg S} ((v_i - t_j) - (s_i - s_j))^2$$

Output                              Source (foreground)

Target (background)

|   |           |   |           |    |           |    |           |
|---|-----------|---|-----------|----|-----------|----|-----------|
| 1 | <b>20</b> | 5 | <b>20</b> | 9  | <b>20</b> | 13 | <b>20</b> |
| 2 | <b>20</b> | 6 | <b>80</b> | 10 | <b>20</b> | 14 | <b>20</b> |
| 3 | <b>20</b> | 7 | <b>20</b> | 11 | <b>80</b> | 15 | <b>20</b> |
| 4 | <b>20</b> | 8 | <b>20</b> | 12 | <b>20</b> | 16 | <b>20</b> |

|   |           |   |           |    |           |    |           |
|---|-----------|---|-----------|----|-----------|----|-----------|
| 1 | <b>10</b> | 5 | <b>10</b> | 9  | <b>10</b> | 13 | <b>10</b> |
| 2 | <b>10</b> | 6 | <b>10</b> | 10 | <b>10</b> | 14 | <b>10</b> |
| 3 | <b>10</b> | 7 | <b>10</b> | 11 | <b>10</b> | 15 | <b>10</b> |
| 4 | <b>10</b> | 8 | <b>10</b> | 12 | <b>10</b> | 16 | <b>10</b> |

|   |           |   |                      |    |                      |    |           |
|---|-----------|---|----------------------|----|----------------------|----|-----------|
| 1 | <b>10</b> | 5 | <b>10</b>            | 9  | <b>10</b>            | 13 | <b>10</b> |
| 2 | <b>10</b> | 6 | <b>v<sub>1</sub></b> | 10 | <b>v<sub>3</sub></b> | 14 | <b>10</b> |
| 3 | <b>10</b> | 7 | <b>v<sub>2</sub></b> | 11 | <b>v<sub>4</sub></b> | 15 | <b>10</b> |
| 4 | <b>10</b> | 8 | <b>10</b>            | 12 | <b>10</b>            | 16 | <b>10</b> |

e.g., pixel  $v_1$       left

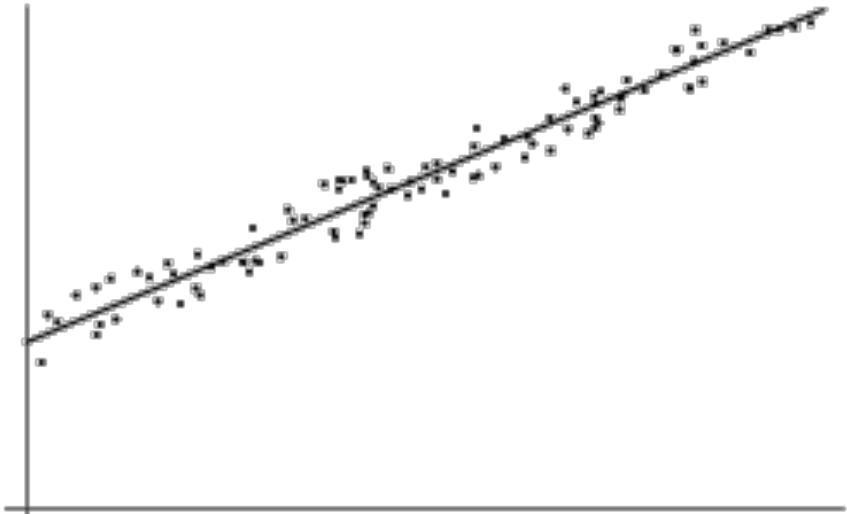
$$((v_1 - 10) - (80 - 20))^2 + ((v_1 - 10) - (80 - 20))^2$$

right                              bottom

$$((v_1 - v_3) - (80 - 20))^2 + ((v_1 - v_2) - (80 - 10))^2$$

# Gradient-domain editing

Creation of image = least squares problem in terms of: 1) pixel intensities; 2) differences of pixel intensities



Least squares line fitting in 2 Dimensions

$$\hat{\mathbf{v}} = \arg \min_{\mathbf{v}} \sum_i (\mathbf{a}_i^T \mathbf{v} - b_i)^2$$

$$\hat{\mathbf{v}} = \arg \min_{\mathbf{v}} (\mathbf{A}\mathbf{v} - \mathbf{b})^2$$

Use sparse linear equation solver in Python and MATLAB

# Examples

## Gradient domain processing

$$\mathbf{v} = \arg \min_{\mathbf{v}} \sum_{i \in S, j \in N_i \cap S} ((v_i - v_j) - (s_i - s_j))^2 + \sum_{i \in S, j \in N_i \cap \neg S} ((v_i - t_j) - (s_i - s_j))^2$$

Source (foreground)

Target (background)

Output

|   |           |   |           |    |           |    |           |
|---|-----------|---|-----------|----|-----------|----|-----------|
| 1 | <b>20</b> | 5 | <b>20</b> | 9  | <b>20</b> | 13 | <b>20</b> |
| 2 | <b>20</b> | 6 | <b>80</b> | 10 | <b>20</b> | 14 | <b>20</b> |
| 3 | <b>20</b> | 7 | <b>20</b> | 11 | <b>80</b> | 15 | <b>20</b> |
| 4 | <b>20</b> | 8 | <b>20</b> | 12 | <b>20</b> | 16 | <b>20</b> |

|   |           |   |           |    |           |    |           |
|---|-----------|---|-----------|----|-----------|----|-----------|
| 1 | <b>10</b> | 5 | <b>10</b> | 9  | <b>10</b> | 13 | <b>10</b> |
| 2 | <b>10</b> | 6 | <b>10</b> | 10 | <b>10</b> | 14 | <b>10</b> |
| 3 | <b>10</b> | 7 | <b>10</b> | 11 | <b>10</b> | 15 | <b>10</b> |
| 4 | <b>10</b> | 8 | <b>10</b> | 12 | <b>10</b> | 16 | <b>10</b> |

|   |           |   |                |    |                |    |           |
|---|-----------|---|----------------|----|----------------|----|-----------|
| 1 | <b>10</b> | 5 | <b>10</b>      | 9  | <b>10</b>      | 13 | <b>10</b> |
| 2 | <b>10</b> | 6 | $\mathbf{v}_1$ | 10 | $\mathbf{v}_3$ | 14 | <b>10</b> |
| 3 | <b>10</b> | 7 | $\mathbf{v}_2$ | 11 | $\mathbf{v}_4$ | 15 | <b>10</b> |
| 4 | <b>10</b> | 8 | <b>10</b>      | 12 | <b>10</b>      | 16 | <b>10</b> |

e.g., pixel  $v_1$   $((v_1 - 10) - (80 - 20))^2 + ((v_1 - 10) - (80 - 20))^2$

Least squares:  $((v_1 - v_3) - (80 - 20))^2 + ((v_1 - v_2) - (80 - 10))^2$

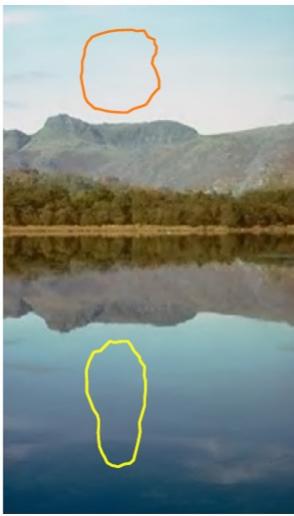
Linear equation:  $4v_1 - 10 - 10 - v_3 - v_2 = (80 - 20) \times 4$

# Perez et al., 2003

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sources



destinations



cloning



seamless cloning



sources/destinations



cloning



seamless cloning



target



source



mask



no blending



gradient domain blending

# What's the difference?



gradient domain blending

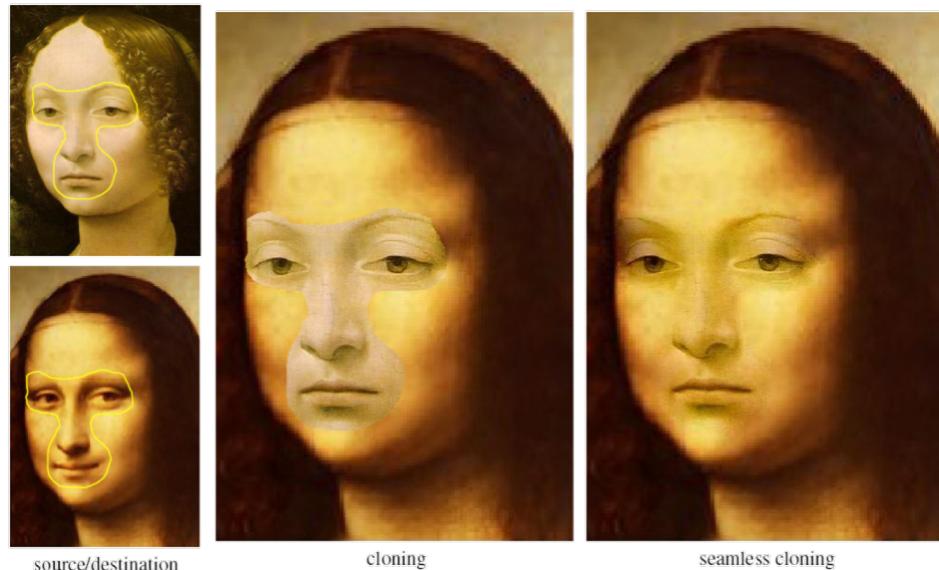


no blending



# Perez et al, 2003

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Local color changes

## Limitations:

- Can't do contrast reversal (gray on black -> gray on white)
- Colored backgrounds "bleed through"
- Images need to be very well aligned

# Drawing in Gradient Domain

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## Real-Time Gradient-Domain Painting

James McCann\*  
Carnegie Mellon University

Nancy S. Pollard†  
Carnegie Mellon University



James McCann & Nancy Pollard  
**Real-Time Gradient-Domain Painting,**  
SIGGRAPH 2009  
(CMU paper)

# Drawing in Gradient Domain

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James McCann & Nancy Pollard  
**Real-Time Gradient-Domain Painting,**  
SIGGRAPH 2009